

Lecture 1

# An Introduction to Population Biology and Modeling

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22 October 2012

- 1 General course info
- 2 Introduction to population biology
  - Population ecology
  - Modeling
- 3 Course outline

# Course Info

- Population ecology, October 2012 - January 2013.
- Language:
  - Slides in English.
  - Lecture and exam in Hebrew.
- Dr. Ido Filin, [ifilin@univ.haifa.ac.il](mailto:ifilin@univ.haifa.ac.il)
- Office hours: Thursday 14:15-16:00,  
Room 241, Multipurpose build.
- Time: Mondays, 08:15-10:00.
- Place: Computer room, Rabin 7036.
- Exam: Open book, in front of computer.
- מועד א': 31 ינואר. מועד ב': 05 מרץ.

# Course Info

- Population ecology, October 2012 - January 2013.
- חובת הגשת תרגילים: 7 תרגילים, אחד כל שבועיים.
- הגשה עד תאריך שבדף התרגיל.
- ציון סופי: 30% תרגילים, 70% בחינה.
- All of the course material will be available on the Highlearn system.
- **Reading:** selected pages from the literature listed in the syllabus, and possibly from other sources.  
Available through HighLearn.

# Outline

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# Prologue: Population within the scales of biology

## **Intracellular processes**

Cell biology, Molecular biology

## **Intraorganismal processes**

Physiology, Developmental biology

## **Whole organism**

Animal behavior

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Ecology



Evolution

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Population genetics

**Species**

Microevolution, Speciation theory

**Higher taxa**

Macroevolution – Paleontology, Taxonomy and Systematics

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Population ecology

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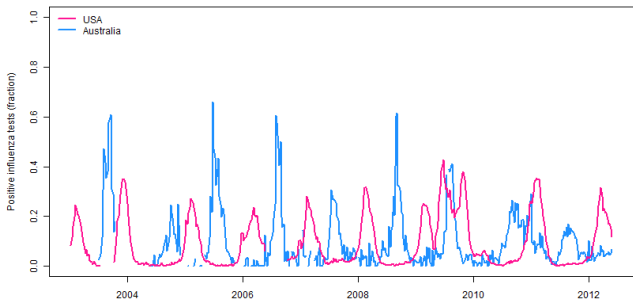
Macroevolution – Paleontology, Taxonomy and Systematics

# Why population ecology?

- Basic science → natural populations exhibit general patterns – research of natural phenomena.
- Conceptual basis for community ecology.
- Analytical tools to compare performance of different organisms, different populations, same organism under different environmental circumstances, etc.
- For example:
  - Controlling growth of microorganisms used in food industry – by varying temperature, pH, etc.
  - Controlling populations of agricultural pests – dose and timing of pesticide application.

# Why population ecology?

- Economic applications
  - Sustainable harvesting – avoiding overexploitation of natural resources; overfishing, overhunting, etc.
  - Human demography – workforce vs. dependents, population aging, infrastructure planning (schools, hospitals, roads, etc.).
- Public health – understanding and controlling outbreaks of disease; vaccination policies.



# Why population ecology?

- Nature conservation – endangered species:
  - Evaluating success – do conservation measures work?
  - Measuring and predicting population recovery or extinction risk.
  - Minimum viable population size.
  - Metapopulations.
- Population ecology provides the conceptual basis for studying evolution by natural selection.

# Modeling in the natural sciences

This course is about mathematical modeling of natural populations.

*The **sciences** do not try to explain, they hardly even try to interpret, they mainly **make models**. By a model is meant a **mathematical construct** which, with the addition of certain verbal interpretations **describes observed phenomena**. The justification of such a mathematical construct is solely and precisely that it is **expected to work**.*

*John von Neumann*

*Essentially, all models are **wrong**, but some are **useful**.*

*George Box*



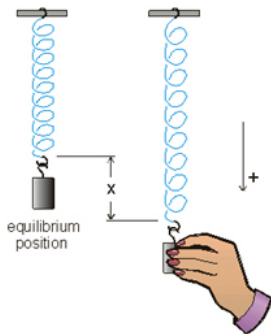
# Modeling in the natural sciences

- Example: Classical Newtonian mechanics is **wrong**.
- It is only an **approximate** description of nature – there is always an error, unexplained phenomenon, or deviation from model-based prediction.
- Newtonian mechanics is not a very good description of nature for very high speeds, very large masses, or at the atomic or molecular scale.
- However, Newtonian mechanics is still **useful** for everyday life: building bridges, designing cars, launching satellites or playing “angry birds”.
- As science progresses, we develop better approximations – in this case, relativity and quantum mechanics.
- But those are still only approximate descriptions – some difference remains between prediction and observation.

# Modeling in the natural sciences

- Science deals with observed phenomena – nature, "reality" – not with truth (whatever truth is).
- Science tries to find general patterns in nature and to describe them – to bring together disparate observations under a unified conceptual framework.
- Sooner or later this process leads to a **mathematical model**.
- A mathematical construct that approximately describes (mimics) nature.
- A mathematical model is **useful** because:
  - 1 It is a **compact description** of a set of observed phenomena.
  - 2 Provides **quantitative** results that can be compared to observed values.
  - 3 Can **predict** future (not yet observed) occurrences of the natural phenomena it attempts to describe.

# State variables: compact description of nature



Mass on a spring.

The state of the system is described by displacement from equilibrium point.

We denote it by  $x$ .

We measure  $x$  in units of length.  
(mm, cm, inches, etc.)

The spring-mass system can be in

Extension state:  $x > 0$ .

Compression state:  $x < 0$ .

Equilibrium state:  $x = 0$ .

By comparing values of  $x$  we can compare different springs, or the state of the same spring in different times.

We can also look for rules in the way  $x$  changes over time  
→ predict the state of the system in the future.

# State variables: compact description of nature

- A **state variable** is that element of the mathematical model that relates to a **property of the natural system** that we are interested in.
- Usually, it relates to a property that changes, or at least may change, over time.
- Examples:
  - $x$  – displacement of the mass-spring system.
  - State of matter: solid, liquid, gas.
  - $p$  – allele frequency in a population.
  - Percentage of infected people in a population.
- Can be continuous:
  - $x = 1\text{cm}, -2.3\text{mm}, 10.9\text{m}.$
  - $p = 0.5, 0.99, 0.01, 1, 0.$
- or discrete:
  - solid/liquid/gas.
  - extended/compressed/at equilibrium.

# State variables: compact description of nature

In population ecology we have two basic state variables:

- 1 Population size,  $N$ .
  - The number of individuals in a population.
  - Discrete,  $N = 0, 1, 2, 3, \dots$
- 2 Population density,  $n$ .
  - The number per unit area/volume.
  - Continuous,  $n = 16.2\text{km}^{-2}, 8673.3\text{cm}^{-3}, \dots$

As populations grow or decline, population size/density changes over time.

# Nature is complex: many state variables

Rarely does a single state variable fully captures the relevant properties of a natural system.

We usually require several. For example:

- A more complete description of the spring-mass system requires both displacement,  $x$ , and velocity,  $v$ .
- A thermodynamic system is described by volume, pressure and temperature.
- Allele frequencies of several alleles/loci/genes.

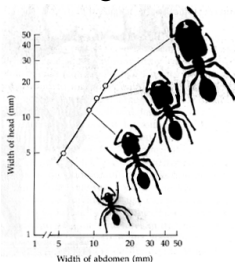
In population ecology:

- Population structure –
  - Age-structure – how many 1yo, 2yo . . . , 80yo . . .
  - Stage-structure – separate numbers for eggs, larvae, juveniles, adults.
- Species interactions – separate population sizes/densities for each species.

# Laws of nature

**Empirical laws** – describe how several state variables change together, or covary.

- Usually derived from observations / data, using statistical analysis, or a good guess.
- Examples:
  - Kepler's third law:  $T_1^2/T_2^2 = R_1^3/R_2^3$
  - Gas law:  $PV = RT$ .
  - Allometry:  $(\text{trait 1}) = a(\text{trait 2})^b \longrightarrow$
  - Other scaling laws.



- It is a static description – does not describe or predict how state variables change over time.
- Only allows to predict the coordinated change in several state variables, if one of them changes.
- Underlying mechanism, or process, is not always known.

# Laws of nature

**Conservation laws** – quantities that remain constant (conserved), despite state changes of the natural system.

- Conservation of mass.
- Conservation of energy.
- Conservation of momentum.
- ...

However, there are very few such quantities.

Most quantities in nature change through time, and in particular, the state variables that describe a natural system.



# Laws of nature

**Dynamics laws** – Provide description of how state variables change or expected to change over time.

Ability to predict future state, based on previous / current observations of the natural system.

They describe specific mechanisms and processes.

Therefore more fundamental and useful than empirical laws.

Often provide the underlying reasons for empirical laws:

- Newton's law of gravitation leads to Kepler's law.
- From kinetic theory of gases we get the gas law.
- Growth gradients lead to allometry.

# Dynamics in discrete vs. continuous time

- We can measure time in **discrete steps**: day 0, day 1, day 2, ...; year 1999, year 2000, year 2001, ...
- Assume we know  $N_t$ , the value of the state variable at time-step  $t$ .
- The value at the next time-step is obtained by a **recursion relation**:  $N_{t+1} = \dots$
- or by a **difference equation**:  $\Delta N = \dots$
- The recursion relation and difference equation are related of course, because  $\Delta N = N_{t+1} - N_t$  and  $N_{t+1} = N_t + \Delta N$ .
- We can repeatedly use the recursion or difference equation to obtain also  $N_{t+2}, N_{t+3}, N_{t+4} \dots$
- And also go backward in time to derive past values:  $N_{t-1}, N_{t-2}, \dots$

# Dynamics in discrete vs. continuous time

- We can also measure time along a **continuous scale**: 21.3 sec since beginning of experiment; 1.7 years since birth, ...
- In such cases, a law of dynamics takes the form of a **differential equation**
- For example, Newton's second law of motion and law of gravitation.
- In mathematical form:  $dN/dt = \dots$
- It describes the time-derivative (= rate of change) of the state variable.
- By solving, we get the the time-trajectory  $N(t)$ .
- $N(t)$  = a function of time that provides the value of the state variable for every value of the time coordinate,  $t$ .

# Dynamics in discrete vs. continuous time

## A note about units.

- In discrete time we have a difference equation:  
(next value) - (current value) = ...
- in continuous time we have a differential equation:  
(rate of change) = ...
- In the former case, we measure change (difference) using the same units as the state variable.
- In the latter case, we measure change as a rate  
→ units of state over units of time.
- Example – the spring-mass system:
  - state variable is displacement,  $x$ , measured in meters (units of length).
  - Discrete time dynamics:  $\Delta x = \dots$ ;  $\Delta x$  also measured in meters.
  - Continuous time dynamics:  $dx/dt = \dots$ ;  $dx/dt$  measured in meters/sec (i.e., units of velocity).

# Dynamics in discrete vs. continuous time


## In population ecology:

- Discrete time dynamics:  $\Delta N = \dots$  ; has no units – a pure number.
- Continuous time dynamics:  $dN/dt = \dots$  ; measured in 1/sec ( or, in general, 1/(unit of time) ).
- If we use density,  $n$ , as a state variable, the units are then, for example,  $\text{km}^{-2}$  and  $\text{km}^{-2}\text{sec}^{-1}$ , respectively.
- The choice of a discrete time vs. continuous time description of a natural population depends on many factors:
  - Seasonal organisms or seasonal breeding vs. breeding year-round.
  - What are we interested in, as scientists – estimates or predictions of population size at specific times? or a continuous time-trajectory of population size?
  - Essentially, all models are wrong. But which description would be more **useful**?

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# Course Outline

- 1 Introduction to population biology and modeling.
- 2 Mathematical modeling, computer simulation, statistical analysis and graphics, using .
- 3 Basic models of population growth – BIDE and geometric/exponential growth – identical individuals, density-independence.
- 4 Discrete time vs. continuous time models.
- 5 Population regulation, density-dependence and intraspecific competition.


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# Course Outline

- 6 Variability among individuals within populations – size-, stage-, age-, state-structure.
- 7 Life tables and life history.
- 8 Comparison and fitting to empirical data – model inference and prediction.
- 9 Population fluctuations and population cycles.
- 10 Stochastic (random) effects in population dynamics; population extinction.
- 11 Community ecology: interspecific competition and predator-prey interaction.



# Course Goals

- 1 Learn fundamental terminology and basic modeling approaches in population ecology.
- 2 Acquire knowledge about the many processes that influence dynamics of natural populations.
- 3 Gain basic skills in mathematical modeling, statistical analysis and graphics, using .

